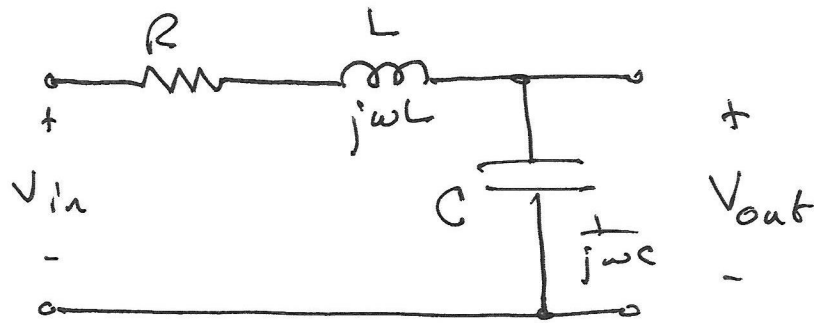


Assume sinusoidal signals.

$$Z_{in} = R + j\omega L + \frac{1}{j\omega C} = R + j\left(\omega L - \frac{1}{\omega C}\right)$$

If  $\omega L = \frac{1}{\omega C}$  then  $Z_{in} = R$  is real



Assume sinusoidal signals.

$$\left. \begin{array}{l} H(j\omega) \\ H(\omega) \end{array} \right\} = \frac{\frac{1}{j\omega C}}{R + j\omega L + \frac{1}{j\omega C}} \cdot \frac{j\omega C}{j\omega C}$$

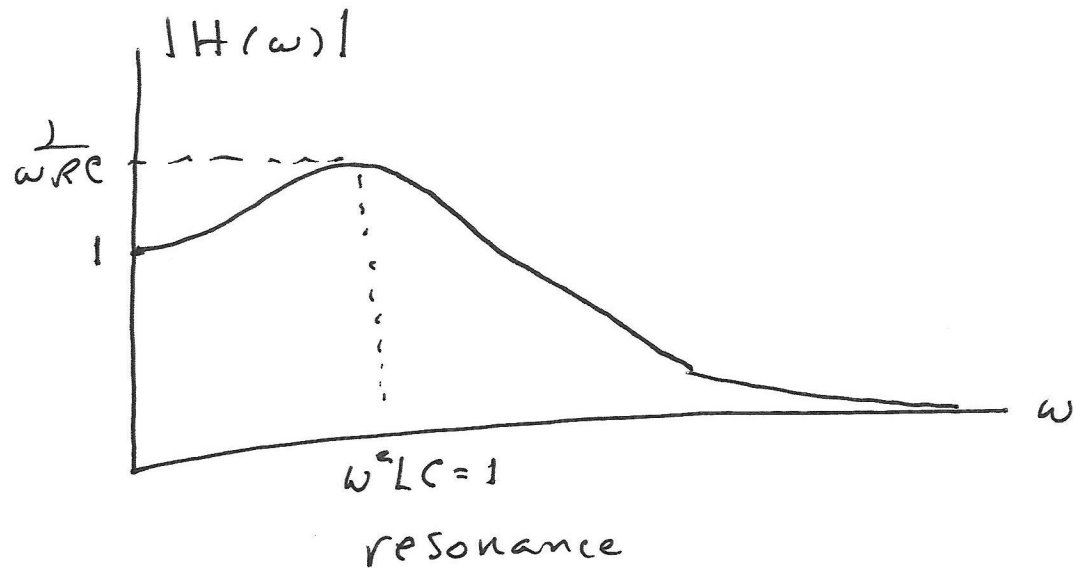
$$= \frac{1}{(1 - \omega^2 LC) + j\omega RC}$$

$$H(\omega) \rightarrow \frac{1}{j\omega RC} \quad \text{as } \omega^2 LC \rightarrow 1$$

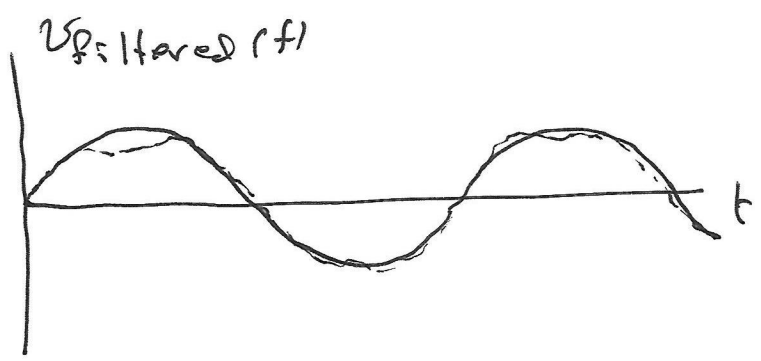
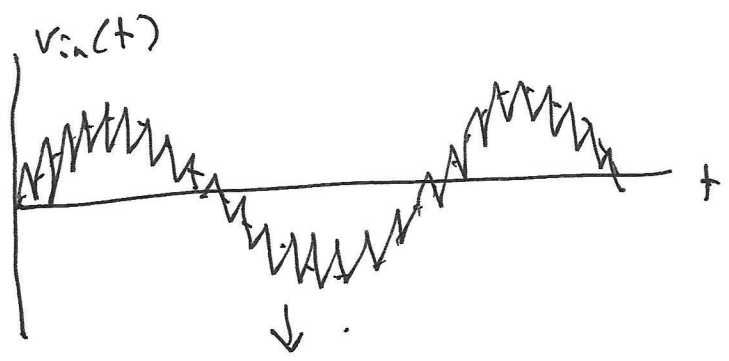
$$H(\omega) = \frac{1}{(1 - \omega^2 LC) + j\omega RC}$$

$$|H(\omega)| = \frac{1}{\sqrt{(1 - \omega^2 LC)^2 + (\omega RC)^2}}$$

$$\rightarrow \frac{1}{\omega RC} \quad \text{as } \omega LC \rightarrow 1$$



$$v_{in}(t) = A_1 \sin 5t + A_2 \sin(100t) + A_3 \sin(1000t)$$



## Operational Amplifier (OpAmp)

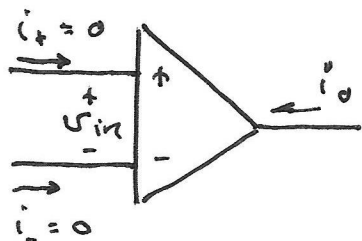
Ideal:

$$V_{in} \approx 0$$

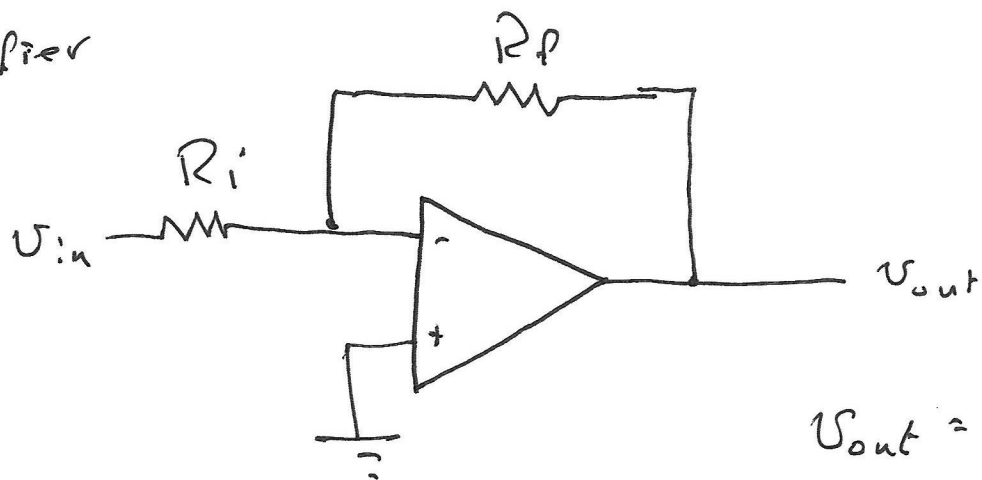
$$i_+ \approx 0$$

$$i_- \approx 0$$

$$i_o = ? \quad (\text{determined by the rest of the circuit.})$$

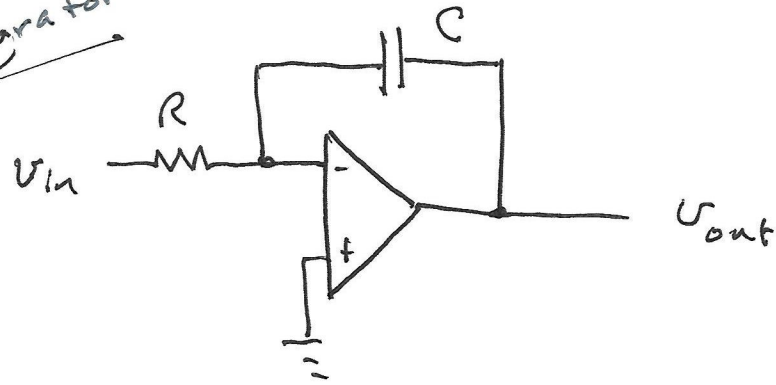


Inverting Amplifier



$$V_{out} = - \frac{R_f}{R_i} V_{in}$$

Integrator

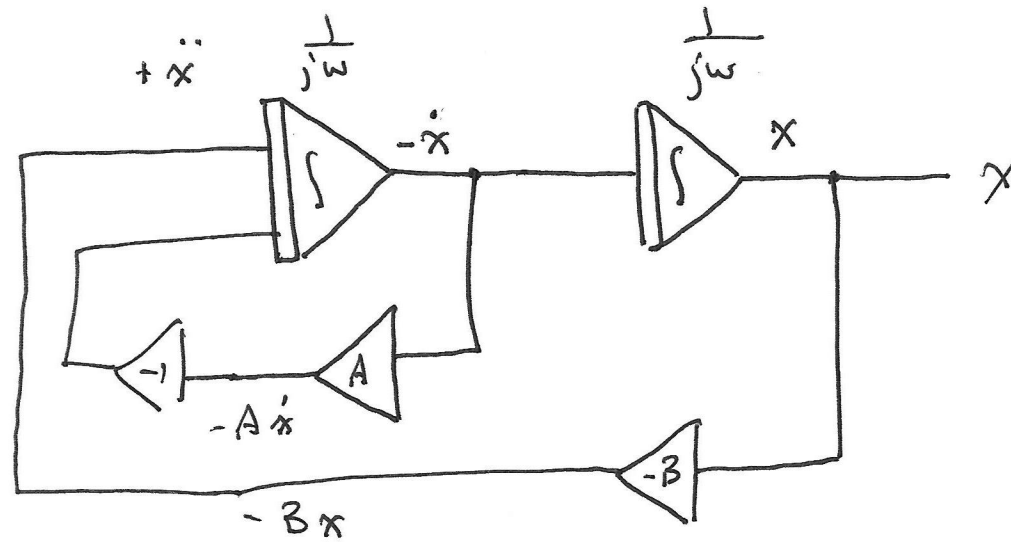


$$v_{out} = -\frac{1}{RC} \int_{-\infty}^t v_{in} dt$$

$$V_{out} = -\frac{1}{j\omega RC} V_{in}$$

$$\ddot{x} + A\dot{x} + Bx = 0$$

$$\ddot{x} = -A\dot{x} - Bx$$



# Complex Numbers

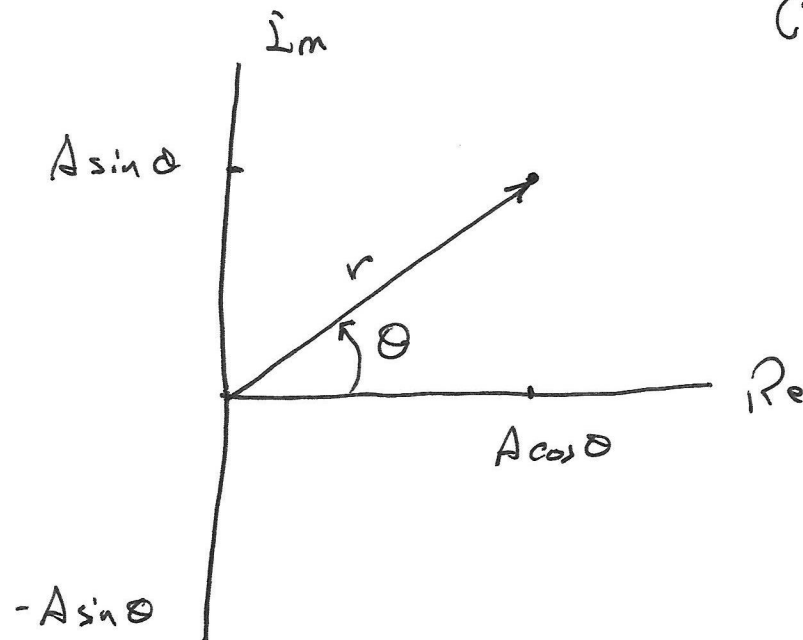
$A \angle \theta$   
polar

$A e^{\pm j\theta}$   
exponential

↓ Euler's  
Identity

$$A (\cos \theta \pm j \sin \theta)$$
$$= A \cos \theta \pm j A \sin \theta$$

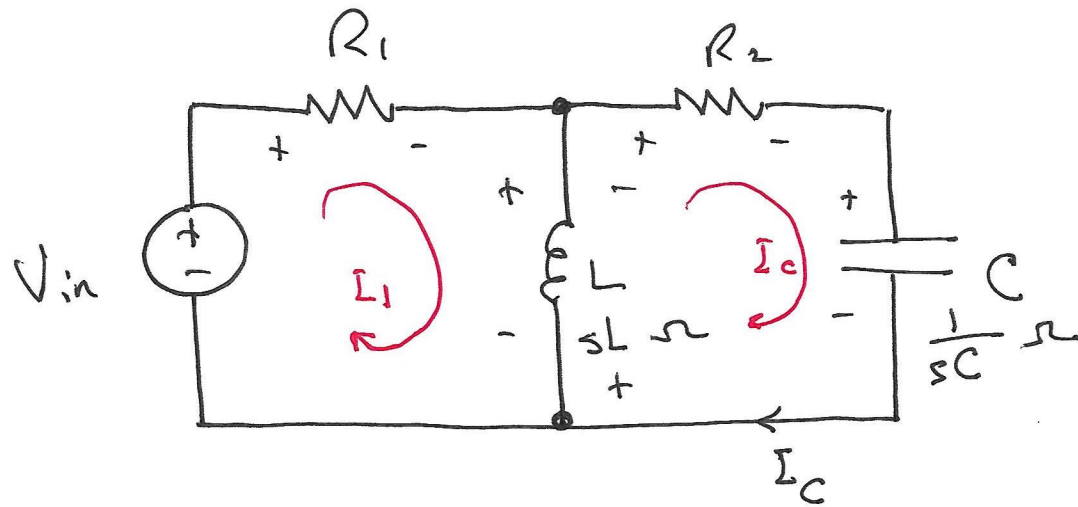
rectangular or  
Cartesian form



$$r = \sqrt{(A \cos \theta)^2 + (A \sin \theta)^2}$$

$$\theta = \tan^{-1} \frac{A \sin \theta}{A \cos \theta}$$
$$= \tan^{-1} \frac{\sin \theta}{\cos \theta}$$



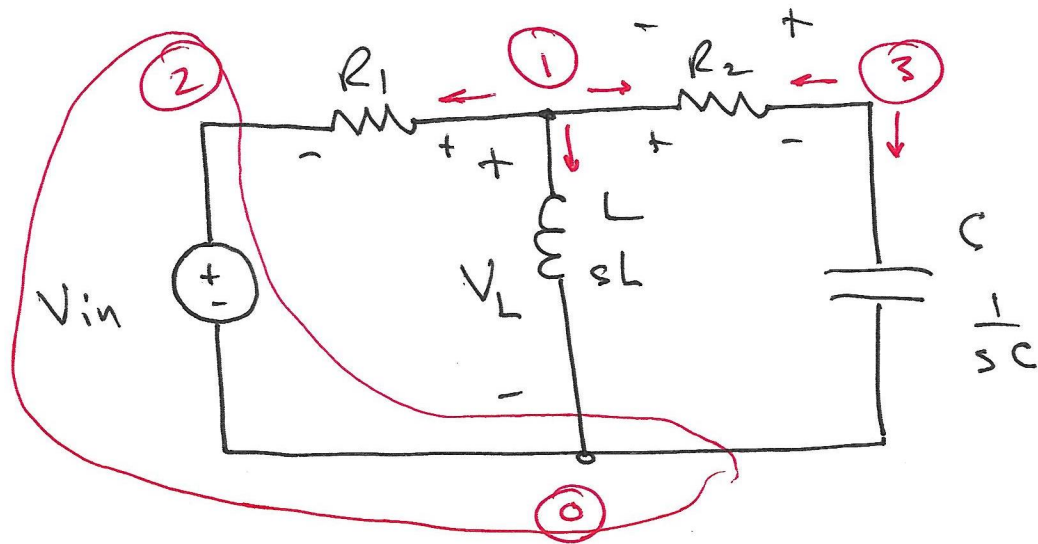


Determine  $I_c$ .

$$R_1 I_1 + sL(I_1 - I_c) = V_{in} \quad \text{KVL for mesh } I_1$$

$$sL(I_c - I_1) + R_2 I_c + \frac{1}{sC} I_c = 0 \quad \text{KVL for mesh } I_c$$

$$\begin{bmatrix} R_1 + sL & -sL \\ -sL & sL + R_2 + \frac{1}{sC} \end{bmatrix} \begin{bmatrix} I_1 \\ I_c \end{bmatrix} = \begin{bmatrix} V_{in} \\ 0 \end{bmatrix}$$



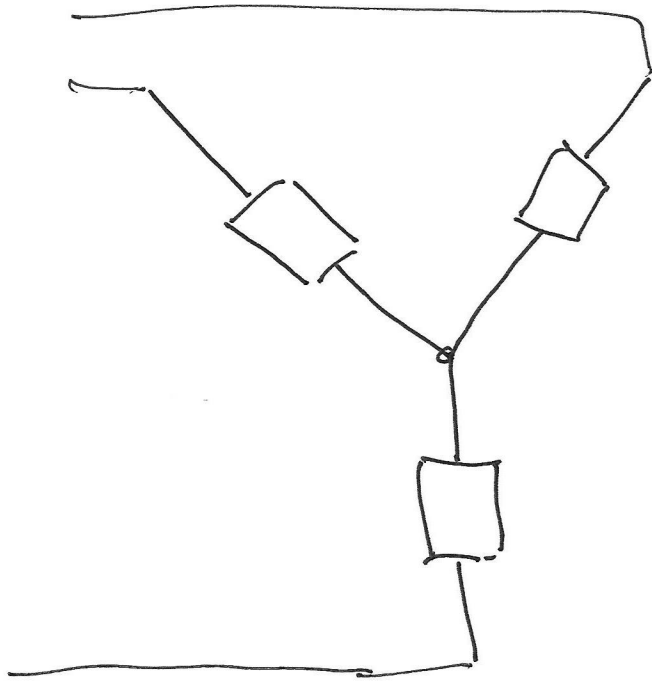
$$V_2 = V_{in} \quad \text{Source constraint}$$

$$\frac{V_1 - V_2}{R_1} + \frac{V_1}{sL} + \frac{V_1 - V_3}{R_2} = 0 \quad \text{KCL for node 1}$$

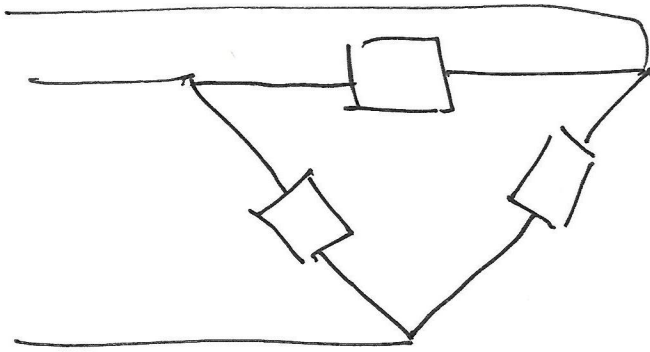
$$\frac{V_3 - V_1}{R_2} + \underbrace{\frac{V_3}{\left(\frac{1}{sC}\right)}}_{= sC V_3} = 0 \quad \text{KCL at node 2}$$

$$\left[ \begin{array}{cc|c} 0 & & 1 \\ \frac{1}{R_1} + \frac{1}{sL} + \frac{1}{R_2} & -\frac{1}{R_1} & 0 \\ -\frac{1}{R_2} & 0 & \frac{1}{R_2} + sC \end{array} \right] \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} V_{in} \\ 0 \\ 0 \end{bmatrix}$$

Solve. Then  $V_L = V_1$ .



wye  
star



delta